

Module 4: Difference-in-Differences and Effects of Medicaid Expansion

Part 2: Basics of Fixed Effects and Panel Data

Ian McCarthy | Emory University
Econ 470 & HLTH 470

Understanding Panel Data

Nature of the Data

- Repeated observations of the same units over time (balanced vs unbalanced)
- Identification due to variation **within unit**

Notation

- Unit $i = 1, \dots, N$ over several periods $t = 1, \dots, T$, which we denote y_{it}
- Treatment status D_{it}
- Regression model,

$$y_{it} = \delta D_{it} + \gamma_i + \gamma_t + \epsilon_{it} \text{ for } t = 1, \dots, T \text{ and } i = 1, \dots, N$$

Benefits of Panel Data

- May overcome certain forms of omitted variable bias
- Allows for unobserved but time-invariant factor, γ_i , that affects both treatment and outcomes

Still assumes

- No time-varying confounders
- Past outcomes do not directly affect current outcomes
- Past outcomes do not affect treatment (reverse causality)

Some textbook settings

- Unobserved "ability" when studying schooling and wages
- Unobserved "quality" when studying physicians or hospitals

Panel Data and Regression

Fixed effects and regression

$$y_{it} = \delta D_{it} + \gamma_i + \gamma_t + \epsilon_{it} \text{ for } t = 1, \dots, T \text{ and } i = 1, \dots, N$$

- Allows correlation between γ_i and D_{it}
- Physically estimate γ_i in some cases via set of dummy variables
- More generally, "remove" γ_i via:
 - "within" estimator
 - first-difference estimator

Within Estimator

$$y_{it} = \delta D_{it} + \gamma_i + \gamma_t + \epsilon_{it} \text{ for } t = 1, \dots, T \text{ and } i = 1, \dots, N$$

- Most common approach (default in most statistical software)
- Equivalent to demeaned model,

$$y_{it} - \bar{y}_i = \delta(D_{it} - \bar{D}_i) + (\gamma_i - \bar{\gamma}_i) + (\gamma_t - \bar{\gamma}_t) + (\epsilon_{it} - \bar{\epsilon}_i)$$

- $\gamma_i - \bar{\gamma}_i = 0$ since γ_i is time-invariant
- Requires strict exogeneity assumption (error is uncorrelated with D_{it} for all time periods)

First-difference

$$y_{it} = \delta D_{it} + \gamma_i + \gamma_t + \epsilon_{it} \text{ for } t = 1, \dots, T \text{ and } i = 1, \dots, N$$

- Instead of subtracting the mean, subtract the prior period values

$$y_{it} - y_{i,t-1} = \delta(D_{it} - D_{i,t-1}) + (\gamma_i - \gamma_{i,t-1}) + (\gamma_t - \gamma_{t-1}) + (\epsilon_{it} - \epsilon_{i,t-1})$$

- Requires exogeneity of ϵ_{it} and D_{it} only for time t and $t - 1$ (weaker assumption than within estimator)
- Sometimes useful to estimate both FE and FD just as a check

Keep in mind...

- Discussion only applies to linear case or very specific nonlinear models
- Fixed effects at lower "levels" accommodate fixed effects at higher levels (e.g., FEs for hospital combine to form FEs for zip code, etc.)
- Fixed effects can't solve reverse causality
- Fixed effects don't address unobserved, time-varying confounders
- Can't estimate effects on time-invariant variables
- May "absorb" a lot of the variation for variables that don't change much over time

Panel Data and Fixed Effects IRL

Within Estimator (Default) in practice

Stata

```
ssc install causaldta  
causaldta gapminder.dta, use clear download  
gen lgdp_pc=log(gdppercap)  
tsset country year  
xtreg lifeExp lgdp_pc, fe
```

R

```
library(fixest)  
library(causaldta)  
reg.dat <- causaldta::gapminder %>%  
  mutate(lgdp_pc=log(gdpPercap))  
feols(lifeExp~lgdp_pc | country, data=reg.dat)
```

Within Estimator (Default) in practice

| Default FE | |
|--------------------|---------|
| Log GDP per Capita | 9.769 |
| | (0.702) |

Within Estimator (Manually Demean) in practice

Stata

```
causaldata gapminder.dta, use clear download  
gen lgdp_pc=log(gdppercap)  
foreach x of varlist lifeExp lgdp_pc {  
    egen mean_`x'=mean(`x')  
    egen demean_`x'=`x'-mean_`x'  
}  
reg demean_lifeExp demean_lgdp_pc
```

R

```
library(causaldata)  
reg.dat ← causaldata::gapminder %>%  
    mutate(lgdp_pc=log(gdpPerCap)) %>%  
    group_by(country) %>%  
    mutate(demean_lifeexp=lifeExp - mean(lifeExp, na.rm=TRUE)  
          demean_gdp=lgdp_pc - mean(lgdp_pc, na.rm=TRUE))  
lm(demean_lifeexp~ 0 + demean_gdp, data=reg.dat)
```

Within Estimator (Manually Demean) in practice

| | Default FE | Manual FE |
|--------------------|-------------------|------------------|
| Log GDP per Capita | 9.769 | 9.769 |
| | (0.702) | (0.701) |

Note: `feols` defaults to clustering at level of FE, `lm` requires our input

First differencing (default) in practice

Stata

```
causaldta gapminder.dta, use clear download  
gen lgdp_pc=log(gdppercap)  
reg d.lifeExp d.lgdp_pc, noconstant
```

R

```
library(plm)  
reg.dat ← causaldta::gapminder %>%  
  mutate(lgdp_pc=log(gdpPercap))  
  
plm(lifeExp ~ 0 + lgdp_pc, model="fd", individual="count")
```

First differencing (manual) in practice

| | Default FE | Manual FE | Default FD |
|--------------------|-------------------|------------------|-------------------|
| Log GDP per Capita | 9.769 | 9.769 | 5.290 |
| | (0.702) | (0.284) | (0.291) |

First differencing (manual) in practice

Stata

```
causaldata gapminder.dta, use clear download  
gen lgdp_pc=log(gdppercap)  
reg d.lifeExp d.lgdp_pc, noconstant
```

R

```
reg.dat ← causaldata::gapminder %>%  
  mutate(lgdp_pc=log(gdpPercap)) %>%  
  group_by(country) %>%  
  arrange(country, year) %>%  
  mutate(fd_lifeexp=lifeExp - lag(lifeExp),  
         lgdp_pc=lgdp_pc - lag(lgdp_pc)) %>%  
  na.omit()  
  
lm(fd_lifeexp~ 0 + lgdp_pc , data=reg.dat)
```

First differencing (manual) in practice

| | Default FE | Manual FE | Default FD | Manual FD |
|--------------------|-------------------|------------------|-------------------|------------------|
| Log GDP per Capita | 9.769 | 9.769 | 5.290 | 5.290 |
| | (0.702) | (0.284) | (0.291) | (0.291) |

FE and FD with same time period

| | Default FE | Default FD | Manual FD |
|--------------------|-------------------|-------------------|------------------|
| Log GDP per Capita | 8.929 | 5.290 | 5.290 |
| | (0.741) | (0.291) | (0.291) |

Don't want to read too much into this, but...

- Likely strong serial correlation in this case (almost certainly)
- Mispecified model